

# Population bias in geotagged tweets

Workshop on Standards and Practices in Large-Scale Social Media Research  
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Slides at [http://mominmalik.com/Malik\\_ICWSM2015\\_slides.pdf](http://mominmalik.com/Malik_ICWSM2015_slides.pdf)

## Motivation

1. All maps of geotagged tweets look like maps of population density
2. LOTS of studies use geotagged tweets
3. Need for large-scale, multivariate, statistical work

## Data

1. Geotags in tweets
2. US Census
3. Mobile users

## Model

1. A statistical test for random distribution over population
2. Validating the null model
3. Spatial autocorrelation and spatial errors
4. Model specification

## Results

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## Discussion

1. Limitations
2. Take-away
3. Future work

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by Eric Fischer  
(<https://www.flickr.com/photos/walkingsf/5985800498>)

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Population density in 2010 US Census. Adapted from  
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We'd like to correct for population density.

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- ▶ Urban life (Doran et al., 2013; Frias-Martinez et al., 2012);
- ▶ Transportation (Wang et al., 2014);
- ▶ Natural disasters, crises, and disaster response (Morstatter et al., 2014; Lin and Margolin, 2014; Shelton et al., 2014; Sylvester et al., 2014; Kumar et al., 2014);
- ▶ Public health (Sylvester et al., 2014; Nagar et al., 2014; Ghosh and Guha, 2013)
- ▶ Language (Hong et al., 2012; Eisenstein et al., 2010; Kinsella et al., 2011);
- ▶ Discourse (Leetaru et al., 2013);
- ▶ Information diffusion/flows (Kamath et al., 2013; van Liere, 2010);
- ▶ Emotion (Mitchell et al., 2013);
- ▶ Social ties (Stephens and Poorthuis, 2014; Takhteyev et al., 2012; Cho et al., 2011)

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Implicit assumption that geotagged tweets tell us about the larger world.  
But do they?

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- ▶ Mislove et al. (2011):
  - ▶ Method: connected user-specified 'location' field to county-level US Census data (data prior to geotags in Twitter)
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- ▶ Pew survey of location services (Zickuhr, 2013):
  - ▶ n=1,178; 'geosocial' n=141; Twitter 'geosocial' n=1
  - ▶ Lowest and middle income use most; lower use less, high use least; more 18-26 year-olds, more Hispanic users

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# Geotags in tweets

What geotags look like:



A screenshot of a tweet from a user in Las Vegas, NV. The tweet text is "This view tho 🤩👉". The location is tagged as "Las Vegas, NV". The image shows a panoramic view of the Flamingo Las Vegas and surrounding city buildings. The tweet has 3 retweets and 42 favorites. The timestamp is 6:17 AM - 1 Apr 2015.

```
https://api.twitter.com/1.1/statuses/show/123456789012345678.json
```

```
{  
  "created_at": "Wed Apr 01 00:47:05  
    +00002015",  
  "text": "This view tho \uE106\uE00E,  
  "user": {  
    "followers_count": 36000,  
    "friends_count": 25000,  
    "geo_enabled": true,  
  },  
  "geo": {  
    "type": "Point",  
    "coordinates":  
      [36.11570625,-115.17407114]  
  }  
}
```

# Geotags in tweets

## About geotags:

- ▶ Latitude and longitude to the ten thousandth of a degree
- ▶ Automatically generated once user enables (unlike 'location')
- ▶ Accessible via Twitter's Streaming API
  - ▶ We used geobox [124.7625, 66.9326]W × [24.5210, 49.3845]N
  - ▶ From April 1 to July 1, 2013, collected **144,877,685** geotagged tweets, representing **2,612,876** unique twitter handles.

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Twitter users sample the population. But the (public) API samples Twitter.

- ▶ API queries for which matches exceed 1% of all tweets are non-randomly sampled (Morstatter et al., 2013)
- ▶ 1.23% of total volume of tweets are geotagged (Liu et al., 2014)
- ▶ US accounts for ~22% of all geotagged tweets (Morstatter et al., 2013)
- ▶  $22\% \times 1.23\% < 1\%$ , so we believe we have everything

# US Census

## Map data:

- ▶ Data are available per “block group”
  - ▶ Block  $\subset$  **Block Group**  $\subset$  Tract  $\subset$  County  $\subset$  State
  - ▶ 220,334 block groups (215,798 in contiguous US).
  - ▶ Unique 12-digit “FIPS” codes
  - ▶ 0.002 square miles to over 7,500 square miles. Designed to have comparable populations (300 to 6,000 people).
- ▶ Block group “shape files” (map file format) are available from Census
- ▶ Use Python `shapely` package to place tweets in block groups.

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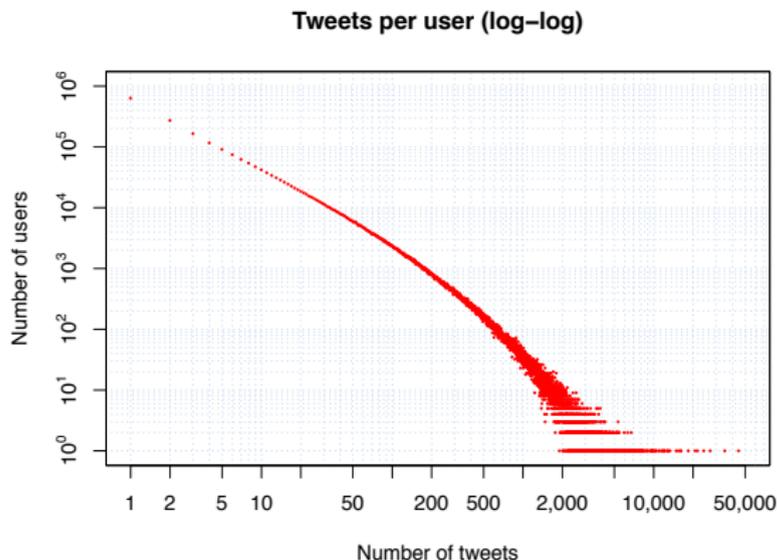
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## Demographic data:

- ▶ 2010 Decennial Census
  - ▶ Tries to count everybody, not sample
  - ▶ Population, Race, Gender, Age, Urban, etc. by block group
- ▶ American Community Survey (ACS)
  - ▶ Done at intervals of 1 year (2013), 3 years (2011-2013), 5 years (2009-2013)
  - ▶ From sampling and inference; only 5-year ACS has block groups
  - ▶ Use this to get median income, which is not in the Census

## Assigning unique locations to mobile users

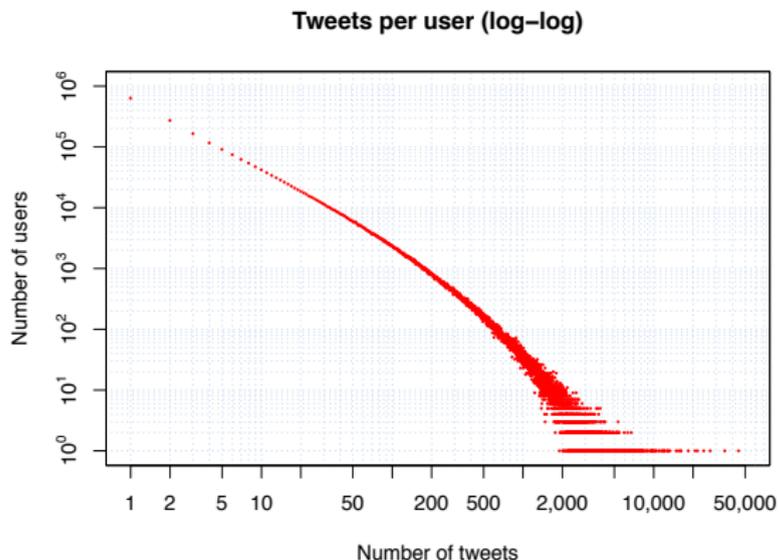
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We also try filtering out users with below 5 geotagged tweets, and users below 10 geotagged tweets. This yields subtly different results.

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Note that  $\log\left(1 + \frac{\varepsilon}{\alpha}\right)$ , very conveniently, now has mean zero. Call this  $\varepsilon'$ .

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This gives us a concrete null hypothesis that we can test,  $H_0 : \beta_1 = 1$ . We will fit the model of eqn (2) and see if we can reject this null.

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log(pop)	1.002*	(0.0003)
Obs.	215,476	
R <sup>2</sup>	0.975	
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F Stat	8,350,415*	
Note:	* $p < 2.2 \times 10^{-16}$	

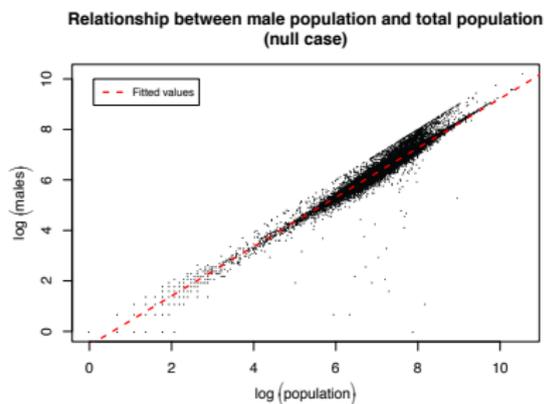
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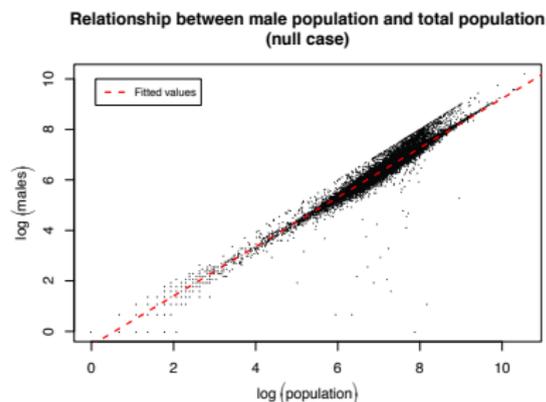
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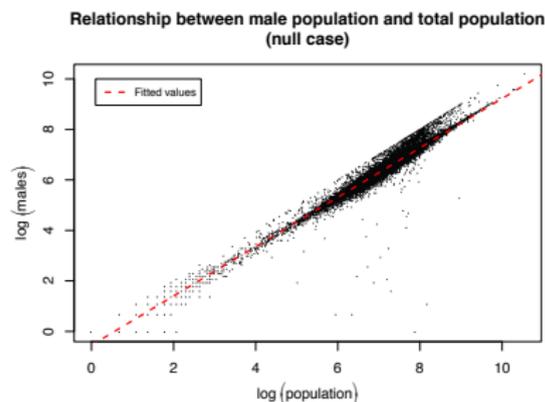
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A 95% CI for the coefficient of log population is  $[1.001, 1.003]$ ; 1 is outside this, but this is without accounting for spatial autocorrelation.

## Spatial autocorrelation

Adjacent geographic units are not independent; there is *spatial autocorrelation*. Measure this with Moran's I,

$$I = \frac{n}{\sum_i \sum_j w_{ij}} \frac{\sum_i \sum_j w_{ij} (X_i - \bar{X})(X_j - \bar{X})}{\sum_i (X_i - \bar{X})^2} \quad (3)$$

which is empirical covariance between adjacent units, appropriately normalized.  $[w_{ij}] = \mathbf{W}$  is an  $n \times n$  matrix of weights (adjacencies between geographic units).

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$\mathbf{W}$  is a substantive modeling choice (Gaetan and Guyon, 2012), but if no prior knowledge, test out different options (Anselin et al., 2007). We try:

- ▶ Rook contiguity; shared edge only (can normalize rows by row sum)
- ▶ Queen contiguity; shared edge or vertex (again, can normalize rows)
- ▶  $k$ -nearest neighbors (using block group centroid) for  $k = 2, \dots, 8$ .

Look for spatial autocorrelation in the residuals of a linear model instead of in individual variables (Anselin and Rey, 1991).

## Spatial errors model

With  $\mathbf{W}$ , correct for spatial autocorrelation in a *spatial errors model*, a type of simultaneous autoregressive (SAR) model.

$$\mathbf{Y} = \mathbf{X}\beta + \mathbf{u} \quad (4)$$

$$\mathbf{u} = \lambda\mathbf{W}\mathbf{u} + \boldsymbol{\varepsilon} \quad (5)$$

where  $\mathbf{u}$  is the vector of correlated residuals,  $\boldsymbol{\varepsilon} \sim \mathcal{N}(\mathbf{0}, \sigma^2\mathbf{I})$  are the uncorrelated error terms, and  $\lambda$  is the strength of the spatial autocorrelation (Anselin, 2002). Equivalently,

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Implemented in R package `spdep` (Bivand and Piras, 2015; Bivand et al., 2013a,b). Fits by finding the log determinant of  $|\mathbf{I} - \lambda\mathbf{W}|$ ; infeasible for  $n = 215,798$ .

Is Cholesky decomposition option, but that requires symmetric matrix, limiting our choices of  $\mathbf{W}$ .

# Model specification

- ▶ Following previous literature, we include covariates for:
  - ▶ Black population, Asian population, Latino/Hispanic populations (Mislove et al., 2011; Zickuhr, 2013)
  - ▶ Age (Longley et al., 2015), binned by ages 10-17, 18-29, 30-49, 50-64, and 65+ (Zickuhr, 2013)
  - ▶ Urban and rural populations (Hecht and Stephens, 2014; Zickuhr, 2013)
  - ▶ Median income (Zickuhr, 2013)
  - ▶ For all of these except median income, stabilize variance with a log transformation and add-one smoothing.

## Model specification

- ▶ Following previous literature, we include covariates for:
  - ▶ Black population, Asian population, Latino/Hispanic populations (Mislove et al., 2011; Zickuhr, 2013)
  - ▶ Age (Longley et al., 2015), binned by ages 10-17, 18-29, 30-49, 50-64, and 65+ (Zickuhr, 2013)
  - ▶ Urban and rural populations (Hecht and Stephens, 2014; Zickuhr, 2013)
  - ▶ Median income (Zickuhr, 2013)
  - ▶ For all of these except median income, stabilize variance with a log transformation and add-one smoothing.
- ▶ We introduce terms for
  - ▶ Northern/eastern effect (demeaned latitudes and longitudes of block group centroids)
  - ▶ Coastal effect (squared terms for latitude and longitude)
- ▶ No analysis of sex as in Longley et al. (2015); Zickuhr (2013); Mislove et al. (2011), as those use name-based inference or survey data, but recall that sex is randomly distributed across block groups.

## Motivation

1. All maps of geotagged tweets look like maps of population density
2. LOTS of studies use geotagged tweets
3. Need for large-scale, multivariate, statistical work

## Data

1. Geotags in tweets
2. US Census
3. Mobile users

## Model

1. A statistical test for random distribution over population
2. Validating the null model
3. Spatial autocorrelation and spatial errors
4. Model specification

## Results

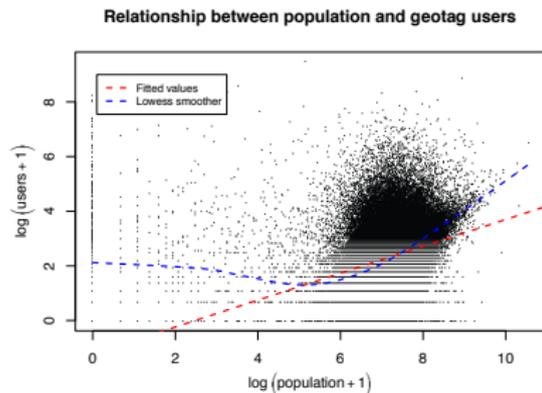
1. Test of null hypothesis
2. Spatial autocorrelation
3. Spatial errors model results

## Discussion

1. Limitations
2. Take-away
3. Future work

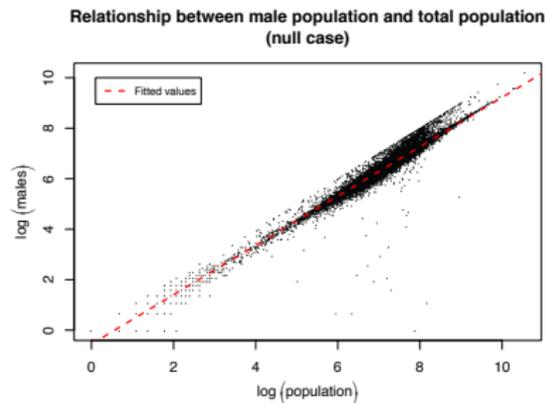
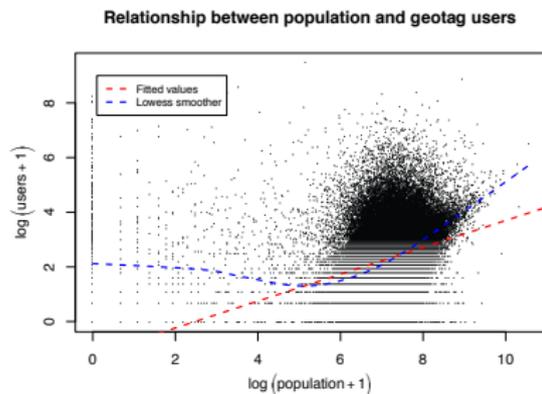
# Test of null hypothesis

Ignoring spatial autocorrelation, and testing  $H_0 : \beta_1 = 0$  with OLS, we get slope  $\hat{\beta}_1 = .4916$  (.002996) and intercept  $\hat{\beta}_0 = -1.219$  (.02143).



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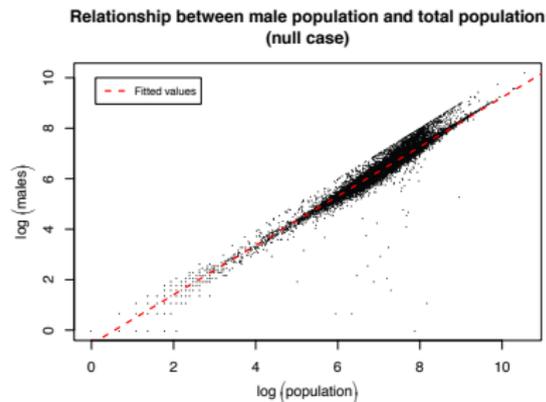
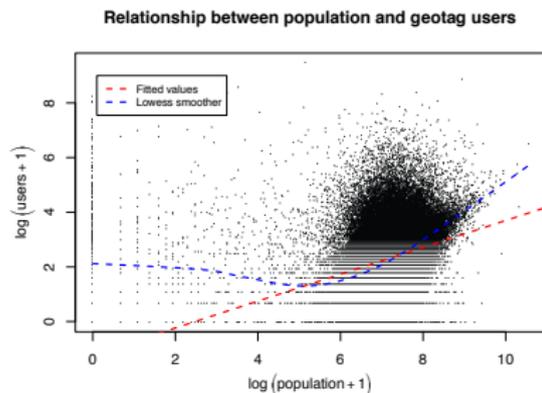
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1 is far outside the 95% confidence interval for  $\beta_1$  of  $[0.4857, 0.4975]$ . Same for only nonzero block groups, and  $>5$ ,  $>10$  tweet filters. No need to worry about spatial autocorrelation; reject the null!

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(Note that we no longer interpret  $\hat{\alpha} = e^{\hat{\beta}_0}$ ).

## Form of spatial autocorrelation

Values of Moran's I in the bivariate regression:

	Population vs Users	Population vs Male
2nn	.3699	.2336
4nn	.3550	.2142
6nn	.3398	.1996
8nn	.3270	.1883
Rook	.4166 (b)	.2125 (b)
	.3992 (rn)	.2201 (rn)
Queen	.4151 (b)	.2097 (b)
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For the Rook contiguity case and the Queen contiguity case, binary (b) and row-normalized (rn) weights give different values. (Nearly identical results for different filter levels).

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All weights pick up spatial autocorrelation. Cholesky decomposition requires a symmetric matrix, so use binary Rook contiguity.

# Spatial errors model results

- No more spatial autocorrelation in residuals

	<i>Dependent variable:</i>	
	log(user+1)	s.e.
log(population+1)	-.01218	(.008081)
log(area)	.1556*	(.001760)
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- The latitude, both in linear and quadratic effects, is not significant.
- Longitude is significant in both effects: block groups further east having more geotag users, and second block groups on both the east and west coasts have more geotag users.

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log(population+1)	-.01218	(.008081)
log(area)	.1556*	(.001760)
log(hispanic+1)	.01533*	(.002066)
log(asian+1)	.1112*	(.001576)
log(black+1)	.04292*	(.001576)
lat (demeaned)	-.006992	(.0007052)
lat <sup>2</sup>	-1.641-e5	(9.505-e5)
long (demeaned)	.02306*	(.0002739)
long <sup>2</sup>	8.777-e5*	(1.411-e5)
med income (\$10K)	.01661*	(.0006857)
log(rural+1)	-.05722*	(.001096)
log(ages 10-17+1)	-.09831*	(.003712)
log(ages 18-29+1)	.3916*	(.004423)
log(ages 30-49+1)	.06362*	(.006731)
log(ages 50-64+1)	-.1793*	(.006953)
log(ages ≥65+1)	.09675*	(.003940)
Intercept	1.3382*	(.1916)

Note: \*p<.0001

- +\$10K median income  $\implies$  +1.66% geotag users.
- Tried to test for median income squared but got computational singularity; visual inspection of plot showed no evidence of nonlinear relationship, and linear effect is weak.
- +1% rural population  $\implies$  -5.72% geotag users, consistent with Hecht and Stephens (2014).
- +1% 18-29 year olds  $\implies$  +39.16% geotag users. Consistent with survey results.
- +1% 50-64 year olds  $\implies$  -17.93% geotag users. Consistent with survey results.
- Teenage population predicts fewer geotag users (than excluded group, ages <10).

# Spatial errors model results

	<i>Dependent variable:</i>	
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- (Intercept not meaningful for log dependent variable.)

## Motivation

1. All maps of geotagged tweets look like maps of population density
2. LOTS of studies use geotagged tweets
3. Need for large-scale, multivariate, statistical work

## Data

1. Geotags in tweets
2. US Census
3. Mobile users

## Model

1. A statistical test for random distribution over population
2. Validating the null model
3. Spatial autocorrelation and spatial errors
4. Model specification

## Results

1. Test of null hypothesis
2. Spatial autocorrelation
3. Spatial errors model results

## Discussion

1. Limitations
2. Take-away
3. Future work

## Limitations

- ▶ Doing things at scale gives lots of statistical power, but we lose the ability to do meaningful visual diagnostics and find interesting outliers
- ▶ We corrected for one type of misspecification, spatial autocorrelation, but there is potentially unexplored structure in the residuals
- ▶ Are other relevant models for dependent/spatial data, such as disease mapping, conditional autoregressive (CAR) models, Gaussian Process regression...
- ▶ 'Plurality' placement yields a few hundred block groups with more users than population; need better way to uniquely locate
- ▶ Don't account for foreign tourists (in 2013, 1 tourist for every 4.5 people in US)
- ▶ Still need assumption that demographics of a block group represent the geotag users there
- ▶ Add-one smoothing can produce some artifacts
- ▶ We don't look at time; we use data from 2010 but tweets from 2013, and geotag trends are almost certainly not stationary
- ▶ This is only for the US; doesn't generalize to any other country

## Take-away

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# Take-away

What are our methodological recommendations?

- ▶ Geotagged tweets are *not* representative. Which means we can't use them to make valid inferences about any larger population.
- ▶ Researchers don't need to stop using geotagged tweets, but we need to stop assuming that results generalize to larger populations and using this assumption as our driving motivation.
- ▶ If we want generalizability, the easiest way to probably to directly demonstrate that we can infer a given external trend from tweets (comes with its own problems...).

# Take-away

What are our methodological recommendations?

- ▶ Geotagged tweets are *not* representative. Which means we can't use them to make valid inferences about any larger population.
- ▶ Researchers don't need to stop using geotagged tweets, but we need to stop assuming that results generalize to larger populations and using this assumption as our driving motivation.
- ▶ If we want generalizability, the easiest way to probably to directly demonstrate that we can infer a given external trend from tweets (comes with its own problems...).
- ▶ We can (and should) still study geotagged tweets, Twitter users, and Twitter...

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- ▶ If we want generalizability, the easiest way to probably to directly demonstrate that we can infer a given external trend from tweets (comes with its own problems...).
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- ▶ If we want generalizability, the easiest way to probably to directly demonstrate that we can infer a given external trend from tweets (comes with its own problems...).
- ▶ We can (and should) still study geotagged tweets, Twitter users, and Twitter... as inherently interesting social and cultural phenomena.
- ▶ We need to take statistical approaches, and many relevant models already exist.

## Future work

- ▶ Re-test with 2013 ACS 1-year estimates: incomplete and lower resolution but more current
- ▶ Repeat analysis in other countries
- ▶ Filter out 'non-personal' users (Guo and Chen, 2014)
- ▶ Filter out foreign tourists by collecting all geotagged tweets or profile info
- ▶ Find better ways to uniquely place users
- ▶ Model demographic differences in different levels of usage
- ▶ Apply other spatial models
- ▶ Long-term spatio-temporal modeling
- ▶ With knowledge of demographic biases, we could model demographic changes

## Thank you! Questions?

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